

# Ada: Provably Reliable

Ada Europe 2013

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# A Ring Buffer: Data

```
1  type Buf_Array is array (0 .. Buf_Size - 1)
2  of Integer;
3  — The array which stores the buffer
4
5  type Ring_Buffer is record
6    Data    : Buf_Array;
7    First   : Integer := 0;
8    Length  : Integer := 0;
9  end record;
10 — The record representing the buffer.
11 — First is the first cell containing valid data.
12 — Length is the number of stored items.
13 — Wrapping around the array borders is possible.
14
15 — The field Length is between 0 and Buf_Size.
16 — The field First is always a valid array index,
17 — hence between 0 and Buf_Size - 1.
```

# Can we do better in Ada?

```
1  type Length_Type is new Integer
2     range 0 .. Buf_Size;
3  — The integer type of buffer length
4
5  subtype Index_Type is Length_Type
6     range 0 .. Length_Type'Last - 1;
7  — The integer type for valid array indices.
8
9  type Buf_Array is array (Index_Type) of Integer;
10
11 type Ring_Buffer is record
12     Data    : Buf_Array;
13     First   : Index_Type := 0;
14     Length  : Length_Type := 0;
15 end record;
```

# A Ring Buffer: API

```
1  function Is_Empty (R : Ring_Buffer)
2  return Boolean;
3  — Check whether the buffer is empty
4
5  procedure Pop (R : in out Ring_Buffer;
6               Element : out Integer);
7  — Return the first element of the buffer,
8  — and remove it from the buffer.
9  — The buffer should not be empty.
10 — The length of the buffer is decreased by one.
```

# Can we do better in Ada 2012? (1/2)

expression functions completely define simple getters in the spec

```
1  function Is_Empty (R : Ring_Buffer)
2  return Boolean
3  is (R.Length = 0);
4  — Check whether the buffer is empty
```

Contracts define the interface between a subprogram and its caller

```
1  function Head (R : in Ring_Buffer)
2  return Content
3  is (R.Data (R.First));
4
5  procedure Pop (R : in out Ring_Buffer;
6               Element : out Integer)
7  with
8    Pre => not Is_Empty (R),
9    Post => not Is_Full (R) and then
10         R.Length = R.Length'Old - 1 and then
11         Element = Head (R'Old);
12 — Remove the returned element from the buffer.
```

# What if a contract is violated?

Contract = assertion

Run-time violation  $\Rightarrow$  run-time exception raised

Pop is passed an empty ring

```
raised SYSTEM.ASSERTIONS.ASSERT_FAILURE :  
failed precondition from ring_buf.ads:53
```

Pop implementation is faulty

```
raised SYSTEM.ASSERTIONS.ASSERT_FAILURE :  
failed postcondition from ring_buf.ads:55
```

# What about static verification? (1/3)

## Limitations of compiler

- Must run quickly → imprecise analysis
- Can detect obvious errors

```
1 procedure P (X : in Integer) with
2   Post => X > 0;
```

postcondition refers only to pre-state

```
1 function F return Boolean with
2   Post => X > 0;
```

function postcondition does not mention result



# What about static verification? (2/3)

## Need for a static verifier

- Precise analysis → longer than compilation
- Scalable analysis → modular, based on contracts
- Can detect subtle errors

```
ring_buf.adb:19:26: range check not proved
```

```
ring_buf.ads:56:21: postcondition not proved
```

# What about static verification? (3/3)

Verifier checks:

- all possible run-time errors
- all user properties (assertions, contracts, invariants)

## Verifier gives complete guarantees

```
ring_buf.ads:37:18: info: postcondition proved
ring_buf.adb:11:36: info: division check proved
ring_buf.adb:12:28: info: range check proved
ring_buf.ads:48:48: info: postcondition proved
ring_buf.adb:19:32: info: division check proved
ring_buf.adb:20:28: info: range check proved
ring_buf.ads:56:21: info: postcondition proved
ring_buf.ads:56:23: info: precondition proved
```

# How does it work?

- A VC (Verification Condition) is generated for every check
  - Based on Hoare logics (1969) -  $\{P\}C\{Q\}$
  - Automated by Dijkstra's calculus (1975)
  - Further automated by Filliâtre's effect computation (1996)
  - Made more efficient by Leino's calculus (2005)
- Each VC is proved separately by calling an SMT prover
  - > alt-ergo ring\_buf.ads\_56\_21\_postcondition.why
  - < Valid

SMT = Satisfiability Modulo Theories

# An example of VC

[...]

```
type length_type
```

```
logic to_int1 : length_type -> int
```

```
axiom range_axiom1 : (forall x:length_type. in_range1(to_int1(x)))
```

```
goal WP_parameter_def :
```

```
(forall r:content map. forall r1:int. forall r2:index_type.  
forall r3:length_type. forall element:content. forall r4:content map.  
forall r5:int. forall r6:index_type. forall r7:length_type.  
forall r8:content map. forall r9:int. forall r10:index_type.  
forall r11:length_type. ((not (is_empty(mk_ring_buffer(mk_buf_array(r, r1),  
r2, r3)) = true)) -> ((((((r4 = r8) and (r5 = r9)) and (r6 = r10)) and  
(of_int1((to_int1(r7) - 1)) = r11)) and (((r = r4) and (r1 = r5)) and  
(of_int2(((to_int2(r2) + 1) % 10000)) = r6)) and (r3 = r7))) and  
(element = get(r, ((to_int2(r2) + r1) - 0)))) ->  
((not (is_full(mk_ring_buffer(mk_buf_array(r8, r9), r10, r11)) = true)) and  
((to_int1(r11) = (to_int1(r3) - 1)) and  
(to_int(element) = to_int(head(mk_ring_buffer(mk_buf_array(r, r1), r2,  
r3))))))))))
```

# What if a VC is not proved?

Various possible causes:

- 1 code is incorrect
- 2 assertion is incorrect
- 3 missing assertions about program behavior
- 4 prover times out
- 5 prover is not smart enough

SPARK 2014 methodology to investigate unproved VCs:  
investigate causes from easier to harder.

## Contrats expressed in Ada

- Code **and** assertions can be executed
- Compiler and verifier fully agree on meaning of assertions  
⇒ code **and** assertions can be tested and debugged

Checks enabled by compiler switches:

- `-gnata`: run-time checking of assertions
- `-gnato`: run-time checking of intermediate overflows

# Investigate missing assertions

The screenshot shows the GPS IDE interface with the following components:

- Project Explorer:** Shows a project named "Search" with a sub-project "Search".
- Source Editor (Left):** Displays the source code for `search.ads`. The `Linear_Search` function is highlighted, with line 35 containing the contract case `A(1) /= Val and then Value_Found_In_Range`.
- Source Editor (Right):** Displays the source code for `search.adb`, showing the implementation of `Linear_Search` and `Linear_Search_Result`.
- Locations Panel:** Shows the location of the contract case at `35:67` in `search.ads`, with the message `contract case not proved`.
- Search Bar:** Located at the bottom, with options for `Regexp` and `Hide matches`.

```
14     when False =>
15       null;
16     end case;
17   end record;
18
19   function Value_Found_In_Range
20     (A : Arr;
21      Val : Element;
22      Low, Up : Index) return Boolean
23   is (for some J in Low .. Up => A(J) = Val);
24
25   function Linear_Search
26     (A : Arr;
27      Val : Element) return Search_Result
28   with
29     Pre => Val >= 0,
30     Post => (if Linear_Search'Result.Found then
31              A (Linear_Search'Result.At_Index)
32              (A(1) = Val =>
33               Linear_Search'Result.At_Index = 1,
34               A(1) /= Val and then Value_Found_In_Range
35               Linear_Search'Result.Found,
36               show path information in Arr'Range => A(J) /= Val) =
37               not Linear_Search'Result.Found);
38   end Linear_Search;
39
40 end Search;
```

```
1 package body Search is
2
3   function Linear_Search
4     (A : Arr;
5      Val : Element) return Search_Result
6   is
7     Pos : Index'Base := A'First;
8     Res : Search_Result;
9   begin
10    while Pos < A'Last loop
11      if A(Pos) = Val then
12        Res := (Found => True,
13               At_Index => Pos);
14        return Res;
15      end if;
16
17      pragma Loop Invariant
18        (Pos in A'Range
19         and then
20          not Value_Found_In_Range (A, Val, A
21          Pos := Pos + 1;
22    end loop;
23
24    Res := (Found => False);
25    return Res;
26  end Linear_Search;
27
28 end Search;
```

Locations

- gnatprove (1 item)
- search.ads (1 item)
- 35:67 contract case not proved

Project Outline Messages Locations Call Trees Entity

## Verifier switches

- `-timeout` increase prover timeout
- `-prover` use alternative SMT prover

Verification can be focused:

- on an individual subprogram or line of code
- both on command-line and inside IDE



# What to do next?

## Traditional fallbacks when proof fails

- manual review
- hand-written proof (automatically assisted)

### Drawbacks:

- require proof & tool expertise
- time consuming, costly
- maintenance problems

⇒ new fallback: testing

## Testing is the last resort for...

- parts of the code that cannot be formally analyzed
- properties that cannot be formalized
- assumptions needed by formal verification

But how to articulate it consistently with formal verification?

New combination provides results **as good as testing alone**  
(at a fraction of the cost!)

## Combined methodology

- subprogram contract captures complete property to verify
- each subprogram is either tested or proved
- testing is done in special mode with additional run-time checks

*Case 1: when proved subprogram  $P$  calls tested subprogram  $T$ , proof depends on correct call result*

*Case 2: when tested subprogram  $T$  calls proved subprogram  $P$ , proof depends on correct calling context*

## Special testing mode in proof context

- precondition of proved function when called in tested
- postcondition of tested function when called in proved
- initialization of in out parameters
- no aliasing of parameters

Checks enabled by compiler switches:

- gnata run-time checking of contracts
- gnateV run-time checking of parameter initialization
- gnateA run-time checking of parameter non-aliasing

Builds upon Ada 2012:

- new specification aspects: contracts, invariants
- new expressions: if-expression, case-expression, quantified expression (for all, for some)
- new attributes: Result, Old

## Examples

```
(if Condition then Expr else Expr)
```

```
(for all Index in Range => Boolean_Expression)
```

```
subtype Multiple is Natural  
  with Dynamic_Predicate => Multiple mod 3 = 0;
```

Main restrictions w.r.t. Ada:

- functions cannot have side-effects
- no pointers (= access types)
- no aliasing (between references)
- no exceptions
- no tasking

## Additional constructs specific to SPARK 2014

**Aspects** Contract\_Cases, Global, Depends

**Pragmas** Loop\_Invariant, Loop\_Variant

**Attributes** Loop\_Entry, Update

Seamlessly integrated in GNAT compiler front-end:

- produces the AST for compilation **and** verification
- analyzes all constructs (generics, contracts, etc.)
- makes all run-time checks explicit in the AST
- gnat2why back-end finally generates Why input for prover

Notable compiler extensions:

- support for new aspects/pragmas/attributes in SPARK 2014
- 3 overflow checking modes → mathematical contracts
- target parametrization → correct proofs for target

# The overflow problem

Example of problem:

- user wants to add two numbers:  $X + Y$
- user wants to assert that addition cannot overflow:  
with `Pre => X + Y in Integer`
- but this expression may overflow itself!

## 3 overflow checking modes

**Strict** Normal overflow checks

**Minimized** Larger base type (64bits) used when needed

**Eliminated** Use bignum library in the remaining cases

- User chooses between 3 modes
- Independent choice for assertions and code
- Same choice for execution and formal verification



**Altran Praxis** confirmed no regression with respect to previous SPARK toolset

**Astrium** assessment on Mission and Vehicle management:  
10 kSLOC, most modules 100 % automatically proved

**All users** consider executable contracts an invaluable help in debugging contract *and* code

More SPARK 2014 material

<http://www.spark-2014.org/>

## New GPL releases: 2013-06-04

### GNAT GPL 2013

- Final touches on Ada 2012 support
- Automatic Endianness conversion ('Scalar\_Storage\_Order)
- Dimensionality checking (new aspects and packages)

### SPARK Hi-Lite GPL 2013

Add-on to GNAT GPL 2013 providing toolset for SPARK 2014

- Larger supported subset of Ada (including generics, discriminants, etc.)
- Same contracts used for testing and formal verification
- Applicable to units partly in SPARK
- Improved automatic proof of complex contracts
- New integration in GPS